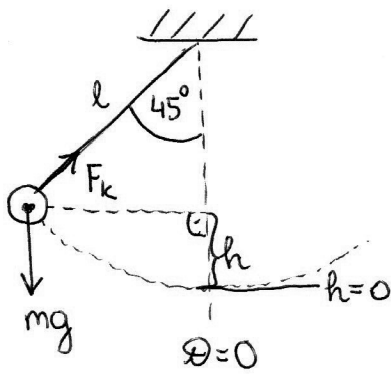


18.)  $\vartheta_0 = 45^\circ$      $a_{\min} = ?$      $\vartheta = ?$



$$a = \sqrt{a_t^2 + a_n^2}$$

$$a_n = \frac{v^2}{l}$$

$$E_M = E_p + E_k$$

$$E_p = mgh$$

$$E_k = \frac{1}{2}mv^2$$

$$a_t = g \sin \vartheta \rightarrow a_t^2 = g^2 \sin^2 \vartheta$$

$$a_n^2 = \frac{v^4}{l^2}$$

$$h = l - l \cos \vartheta = l(1 - \cos \vartheta)$$

$$E_M = \text{all}$$

$$mgh_0 = mgh + \frac{1}{2}mv^2 \rightarrow v^2 = 2g(h_0 - h) = 2g(l - l \cos \vartheta_0 - l + l \cos \vartheta)$$

$$v^2 = 2gl(\cos \vartheta - \cos \vartheta_0)$$

$$a_n = \frac{v^2}{l} = 2g(\cos \vartheta - \cos \vartheta_0)$$

$$a^2 = a_t^2 + a_n^2 = g^2 \sin^2 \vartheta + 4g^2 (\cos \vartheta - \cos \vartheta_0)^2 = \dots$$

$$a^2 = 3g^2 \cos^2 \vartheta - 8g^2 \cos \vartheta_0 \cos \vartheta + g^2 + 4g^2 \cos^2 \vartheta_0$$

Minimális  $\vartheta$ -nál, ha  $\frac{da^2}{d\vartheta} = 0$

$$\frac{da^2}{d\vartheta} = 3g^2 \cdot 2 \cos \vartheta (-\sin \vartheta) - 8g^2 \cos \vartheta_0 (-\sin \vartheta) = 0$$

$$\vartheta_1: \sin \vartheta_1 = 0$$

$$\vartheta_1 = 0$$

$$\vartheta_2: 6g^2 \cos \vartheta_2 - 8g^2 \cos \vartheta_0 = 0$$

$$\cos \vartheta_2 = \frac{4}{3} \cos \vartheta_0$$

egyik minimum, másik maximum

Behelyettesítve eldönteni...